

Learning Continuous Action Models in a Real-Time Strategy Environment

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Abstract

Although several researchers have integrated methods for reinforcement learning (RL) with case-based reasoning (CBR) to model continuous action spaces, existing integrations typically employ discrete approximations of these models. This limits the set of actions that can be modeled, and may lead to non-optimal solutions. We introduce the Continuous Action and State Space Learner (CASSL), an integrated RL/CBR algorithm that uses continuous models directly. Our empirical study shows that CASSL significantly outperforms two baseline approaches for selecting actions on a task from a real-time strategy gaming environment.

1. Introduction

Real-time strategy (RTS) games are a popular recent focus of attention for AI research (Buro 2003), and competitions now exist for testing intelligent agents in these environments (e.g., AIIDE 2007; NIPS 2008). RTS environments are usually partially observable, sequential, dynamic, continuous, and involve multiple agents (Russell and Norvig 2003). Typically, each player controls a team of units that can gather resources, build structures, learn technologies, and conduct simulated warfare, where the usual goal is to destroy opponent units. Popular RTS environments for intelligent agent research include Wargus (Ponsen et al. 2005), ORTS (Buro 2002), and MadRTS, a game developed by Mad Doc Software, LLC.

A main attraction of RTS environments is that they can be used to define and provide feedback for challenging real-time control tasks (e.g., controlling single units, winning an entire game) characterized by large, continuous action and state spaces. However, the vast majority of intelligent agent research with RTS environments relies on discretizing these spaces (see §2.2). This process biases the learner, and may render optimal actions inaccessible.

In this paper, we describe CASSL (Continuous Action and State Space Learner), an algorithm that integrates case-based reasoning (CBR) and reinforcement learning (RL) methods that do not discretize these spaces. We demonstrate and analyze CASSL's utility in the context of a task defined in MadRTS. Although previous research exists on continuous action and state spaces, as well as on CBR/RL integrations, we believe ours is unique in how it generates actions from stored experience.

Section 2 includes a brief introduction to the real-time strategy environment we use along with a summary of related research. In Section 3, we introduce CASSL and explain how it extends our previous research. Section 4 describes an evaluation of its utility in comparison with simpler approaches. Finally, in Section 5 we provide greater context for interpreting these results.

2. Background: Domain and Related Work

2.1 Real-Time Strategy Domain

In this paper, we focus on performance tasks whose space of possible actions A and state space S are multi-dimensional and continuous. We use MadRTS, whose engine is also used in the *Empire Earth II*TM game, for our evaluation. We also considered using Wargus, but chose to use MadRTS because it is more reliable and supports scenarios with higher military relevance.

We created MadRTS scenarios to test the capabilities of intelligent agents for controlling a set of units using a feature-vector representation. Figure 1 shows a snapshot of one of these scenarios, in which the units to be controlled are the soldier units in the lower left corner. Their task is to eliminate the opposing units in the scenario, which are located in the top left and lower right corners. An action in this space corresponds to an order given by the agent to a group of units. Each order directs the soldiers to travel along a vector starting at their current position, attacking any opponent units they encounter after completing this movement. The lengths of these movements are variable, so some actions have longer durations than others. We evaluate an agent based on how many orders it gives, not how much time it requires to complete a task.

The four dimensions of the continuous action space are:

- Heading $\in [0^\circ, 360^\circ]$, where 0° is the heading from the original midpoints of player and opponent soldiers
- Distance $\in [0, d]$, where d is the longest traversable distance in the scenario
- Group size $\in [0, g]$, where g is the number of controllable units in the scenario
- Group selection $\in \{\text{all, strongest, leastRecent}\}$, where the values indicate the method used to select a group

The state space consists of eight features, which are defined relative to the midpoint of the player's units:

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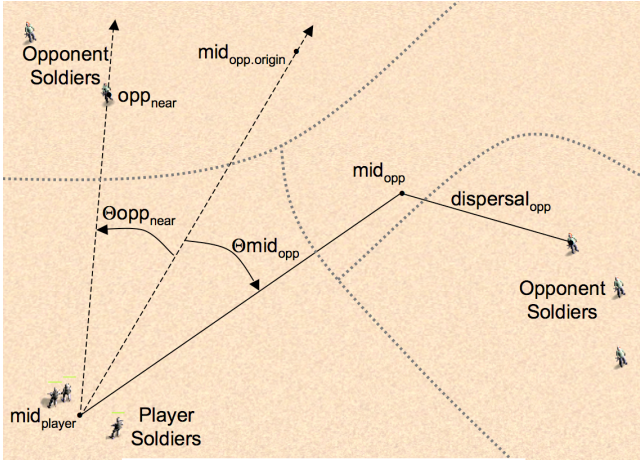


Figure 1: The MadRTS State Space

- Percentage of player’s initial soldiers still alive
- Percentage of opponent’s initial soldiers still alive
- Percentage of territories owned by the player
- Heading to nearest opponent soldier $\in [0^\circ, 360^\circ]$
- Heading to midpoint of opponent soldiers $\in [0^\circ, 360^\circ]$
- Distance to midpoint of enemy soldiers $\in [0, d]$
- Dispersal of opponent soldiers $\in [0, d]$, defined as the median of distances from each opponent soldier to the midpoint of all opponent soldiers
- Dispersal of player soldiers $\in [0, d]$

At each time point, the agent receives a state vector with the values of these features and selects an action to execute. For example, in Figure 1, the player units are at their initial location in the lower left corner, and the opponents are in the upper left and lower right corners. For both sides, the percentage of original soldiers remaining is 100% and the percentage of territories (borders shown by dotted lines) owned is 25%. The heading to the nearest opponent soldier is shown by Θ_{opp_near} . The heading to the midpoint of opponent soldiers is Θ_{mid_opp} and the distance to their midpoint is shown as a line from mid_player to mid_opp . The dispersal of opponent soldiers is labeled $disp_opp$, while the (small) dispersal of player soldiers is not shown.

2.2 Related Work

Several techniques for decision making have been tested in RTS environments, including relational Markov decision processes (Guestrin et al. 2003), integrated scheduling and means-ends analysis planning (Chan et al. 2007), and simulation combined with Nash equilibrium approximation (Sailer, Buro, and Lanctot 2007).

CBR and RL approaches have also been investigated separately for RTS planning tasks. For example, CBR techniques have been designed to select action sequences (Aha, Molineaux, and Ponsen 2005) and to construct plans from behavioral cases extracted from and annotated by human players (Otañón et al. 2007). RL techniques have been used to select: action sequences (Ponsen et al. 2006), choices defined in partial programs (Marthi et al. 2005), and challenge-sensitive actions (Andrade et al. 2005). Un-

like these previous methods, CASSL does not discretize the action space, and uses an integrated CBR/RL approach to select primitive actions in an RTS task.

Previous approaches for learning in the context of continuous action spaces have been investigated separately for CBR and RL methods. Among example CBR approaches, Aha and Salzberg (1994) examined a set of supervised learning approaches for a ball-catching task. Their algorithms restricted action selection to among those that had been previously recorded, which limits the set of actions that can be selected for a new state. Sheppard and Salzberg (1997) describe a lazy Q -learning approach for action selection for a missile avoidance task in which the set of states whose distance is within a threshold are located, and among those the action is selected that has the highest Q value. CASSL instead applies a quadratic model to the nearest neighbors and selects an action corresponding to its maximum. This differs from locally weighted regression (Atkeson, Moore, and Schaal 1997), which computes a local *linear* model from a query’s neighboring cases.

Traditionally, RL methods have used *eager* learning methods to help select actions from continuous action spaces (Kaelbling, Littman, and Moore 1996, §6.2). For example, these include training a neural network with state-action input pairs and Q value outputs, and then applying gradient descent to locate actions with high Q values. Alternatively, this network could be used with an active learning process to test actions generated according to a distribution whose mean and variance were varied so as to find a local maximum. Gaskett et al. (1999) describe an eager approach that performs interpolation with a neural network’s outputs. They also survey continuous action Q -learning systems and note that most are eager and yield piecewise-constant functions. In contrast, our approach uses a lazy method for action selection and is not restricted to piecewise-constant action-selection functions.

Takahashi et al. (1999) instead tessellate a continuous action space in their Q -learning extension. CASSL does not rely on decomposing the action space. Millán et al. (2002) investigate a Q -learner that explores a continuous action space by leveraging the Q -values of neighboring, previously-explored actions. However, this limits action selection to the set of previously explored actions. Buck et al. (2002) heuristically select a set of actions that are distributed across the action space and select the one corresponding to the maximum-valued successor state. CASSL instead selects actions used in neighbor states, dynamically forms a quadratic model from them, and selects the action that yields a maximum value according to this model.

Sharma et al. (2007) integrated CBR and RL techniques in CARL, a hierarchical architecture that uses an instance-based state function approximator for its reinforcement learner and RL to revise case utilities. They also investigated its application to scenarios defined using MadRTS. However, CARL’s action space is discrete, whereas our contribution is an integrated method for reasoning with continuous action spaces. Santamaria et al. (1997) also examined integrated CBR/RL approaches that operate on

continuous action spaces and applied them to non-adversarial numeric control tasks. For example, this included a CMAC (Albus 1975) approach for Q -learning that discretizes the set of possible actions and selects the action with the highest Q -value. In contrast, CASSL dynamically optimizes a continuous local model of the action-value space, which allows access to all potential actions without requiring a search over all of them.

Finally, unlike other Q -learning extensions that select from among the actions in the (state) neighbors to a query, Hedger (Smart & Kaelbling 2000) fits a quadratic surface and selects an action that maximizes it. While CASSL also calculates a regression surface, it is based on the value of states that would occur *if the state changed according to trajectories observed in the past*. Although these past trajectories may be inaccurate for the current state, the values predicted are influenced less by nearby cases, and provide a more diverse basis for the regression surface.

3. Continuous Action and Space Learning

We now describe CASSL (Continuous Action and Space Learner), which integrates case-based and reinforcement learning methods to act in an environment with continuous states and actions. CASSL leverages our experiences with CaT (Aha et al. 2005), which uses CBR techniques (but not RL) to control groups in Wargus (Ponsen et al. 2005), a dynamic, non-episodic, and nearly deterministic RTS environment. CaT’s control decisions focus on tactic selection, where tactics are comparatively long sequences of primitive actions lasting a significant fraction of a trial.

3.1 Motivation for this Integrated Approach

CaT has two limitations that CASSL addresses. First, CaT was designed for an abstract action space (i.e., it selects from among a small set of pre-defined tactics) and required a large state-space taxonomy; it was not designed for a knowledge-poor continuous action domain or, more generally, domains that have a large number of primitive actions. Techniques that make decisions of smaller granularity may permit greater control, and eliminate the need for creating tactics in advance. Greater control may also increase task performance and reduce dependence on an external source of tactics. For example, suppose CaT’s opponent tries to gain an advantage via early use of air units. If none of CaT’s tactics can create air units early on, it will probably lose often. With direct access to primitive actions that create new units, CASSL is not prone to this problem.

Second, CaT cannot reason about causal relations among states, which can be used to improve credit assignment. Standard RL techniques for representing value functions and action-value functions can represent these relations (Sutton and Barto 1998), which motivates our investigation of an integrated CBR/RL approach in this paper. For example, if CaT tends to pick a poor-performing tactic subsequent to a good tactic, then it would average the performance across all successor tactics. In contrast, CASSL instead uses a sample backup procedure that can more quickly improve the accuracy of performance approximations.

3.2 CASSL Algorithm

CASSL is a case-based reasoner that responds to each time step of a game trial by executing a function *LearnAct*,

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T: Transition case base <S × A × ΔS>
V: Value case base <S × ℝ>
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LearnAct( $s_{i-1}, a_{i-1}, s_i, r_{i-1}$ ) =
  T ← retainT( $T, s_{i-1}, a_{i-1}, s_i - s_{i-1}$ )      ; Update transition case base
  V ←
    retainReviseV( $V, s_{i-1}, \text{retrieve}(V, s_i)$ ) ; Update value case base
    C ← retrieve( $T, s_i$ )                        ; Retrieve similar transition cases
    M ← ∅                                       ; Initialize the map of actions to values
    ∀ c ∈ C: M ←                               ; Populate it for retrieved cases' actions
      M ∪ <c.a, retrieve( $V, s_i + c.Δs$ )>
    a_i ← arg max a ∈ A reuse(M, a)           ; Fetch action w/ max predicted reward
    return a_i                                using the Nelder-Mead simplex method

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Figure 2: CASSL’s learning and action selection function

which updates CASSL’s case bases and returns a new action to be performed. *LearnAct* inputs a prior state $s_{i-1} \in S$, an action $a_{i-1} \in A$ which was taken in state s_{i-1} , the state $s_i \in S$ which resulted from applying a_{i-1} in s_{i-1} , and a reward $r \in \mathbb{R}$. It outputs a recommended action $a_i \in A$. States in S and actions in A are represented as real-valued feature vectors.

Figure 2 details CASSL’s *LearnAct* function. It references two case bases, which are updated and queried during an episode. The first is the **transition case base** T : $S \times A \times \Delta S$, which models the effects of applying actions. T contains observed state transitions that CASSL uses to help predict future state transitions. These have the form:

$$c_T = \langle s, a, \Delta s \rangle$$

The second case base is the **value case base** V : $S \times \mathbb{R}$, which models the value of a state. It contains estimates of the sum of rewards that would be achieved by CASSL starting in a state s and continuing to the end of a trial using its current policy. Value cases have the form:

$$c_V = \langle s, v \rangle$$

Each of CASSL’s two case bases supports a case-based problem solving process consisting of a cycle of case retrieval, reuse, revision, and retention (Aamodt and Plaza 1994). These cycles are closely integrated because a solution to a problem in T forms a problem in V ; CASSL solves these problems in tandem to select an action.

At the start of a trial each of CASSL’s case bases is initialized to the empty set. CASSL retains new cases and revises them through its application to a sequence of game-playing episodes. For each new state s_i that arises during an episode, *LearnAct* is called with its four arguments.

LearnAct begins with a case retention step in T ; if an experience occurs that is not correctly predicted by T , a new case $c_{T,i} = \langle s_{i-1}, a_{i-1}, \Delta s \rangle$ is added, where $\Delta s = s_i - s_{i-1}$ (a vector from the prior to the current state). Retention is controlled by two parameters τ_T , and σ_T (not shown in Figure 2); $c_{T,i}$ is retained if either the distance $d_T(c_{T,i}, \text{INN}(V, c_{T,i}))$ between $c_{T,i}$ and its nearest neighbor in T is less than τ_T , or if the distance $d_T(c_{T,i}, \Delta s, T(s_{i-1}, a_{i-1}))$ between the actual and the estimated transitions is greater than the maximum error per-

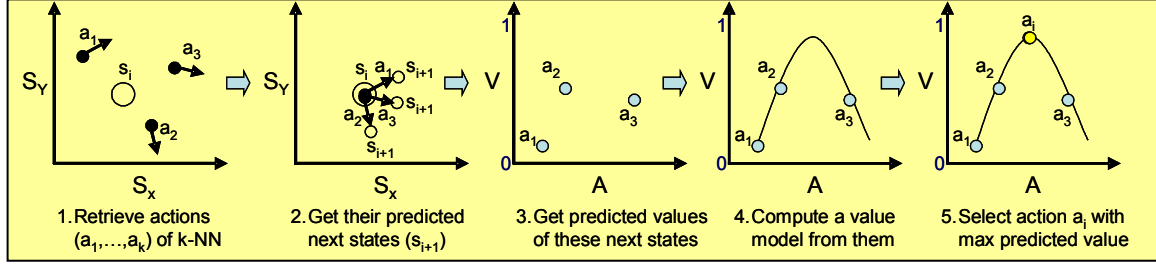


Figure 3: CASSL's algorithm for action recommendation, where S_x and S_y are hypothetical state features

mitted, σ_T . Transition cases are never revised, under the assumption of a deterministic environment.

The second line in *LearnAct* performs conditional case retention and revision for V . A new case $c_{v,i}$ is added to V only if the state distance $d_V(c_{v,i}, \text{INN}(V, c_{v,i}))$ to its nearest neighbor in V is greater than τ_V (not shown in Figure 2). New cases are initialized using the discounted return (Sutton and Barto 1998):

$$c_{V,i} = \langle s_{i-1}, \sum_{k=i}^{\infty} \gamma^k r_{k+1} \rangle$$

Otherwise, $c_{v,i}$'s k -nearest neighbors are revised to better approximate the actual value of this region of the state space. The state value v_k associated with each nearest neighbor $c_{v,k} \in \text{kNN}(V, c_v)$ is revised according to its contribution to the error in estimating the value of v_{i-1} :

$$v_k = v_k + \alpha(r_{i-1} + \gamma v_i - v_k) \star \frac{K(d(c_{V,i}, c_{V,k}))}{\sum_{c_{V,j} \in \text{kNN}(V, c_v)} K(d(c_{V,i}, c_{V,j}))}$$

where v_k is the value associated with neighbor $c_{v,k}$, α ($0 \leq \alpha \leq 1$) is the learning rate, γ ($0 \leq \gamma \leq 1$) is a geometric discount factor, and the Gaussian kernel function $K(d) = \exp(-d^2)$ determines the relative contributions of the k -nearest neighbors.

Figure 3 summarizes the remaining (action-recommendation) steps of *LearnAct*, which next retrieves C , the set of transition cases in T whose states are similar to s_i . This identifies states that are reachable from the current state, and actions for transitioning to them (see step 1 in Figure 3). CASSL uses a simple k -nearest neighbor algorithm on states for case retrieval. However, we set k to be large so as to retrieve enough information for the later regression step to succeed. Specifically:

$$k \geq \frac{|a|^2}{2} + |a| + 1,$$

where $|a|$ is the size of an action vector.

Next, for each nearest neighbor $c_{T,k} = \langle s_k, a_k, \Delta s_k \rangle$, CASSL computes the predicted next state that results from applying a_k in state s_i , thus creating a mapping M from actions to the value of the expected resulting state. This value is calculated by performing the vector addition $\Delta s_k + s_i$, which yields the predicted state s_{i+1} . Then V is reused to calculate the expected value of state s_{i+1} (step 3 in Figure 3). Retrieval and reuse are performed in the same fashion

as described for the step that updates V .

CASSL then creates a multi-dimensional model of this action-value map using quadratic regression (step 4 in Figure 3), which is necessary due to the continuous nature of the state and action spaces. We chose quadratic regression because a quadratic function often produces a useful peak that is not at a point in the basis mapping, thereby encouraging exploration. Higher orders of regression may also produce such results, but are more computationally expensive, and we would like to produce a result in real time.

The final step locates the action that maximizes this model, and adds it to M . To compute this, we use Flanagan's (2007) implementation of the Nelder-Mead simplex method, a well-known method for finding a maximum value of a general n -dimensional function.

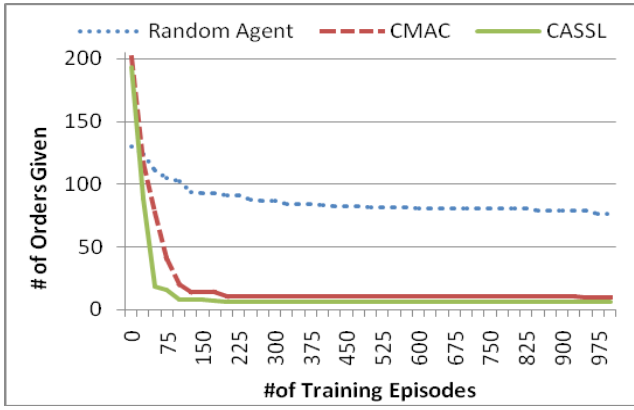
The quadratic estimate of the value of the discovered action is less accurate than a case-based prediction. Thus, we

iteratively re-create the model, incorporating more accurate predictions, by repeating Steps 4 and 5 (Figure 3) until a similar action is found on two successive iterations, or until 50 iterations have passed. Similarity between successive actions is defined as a Euclidean distance less than a small threshold value; we use 0.0001 as the threshold.

4. Evaluation

Our empirical study focuses on analyzing whether CASSL's continuous action model significantly outperforms a similar algorithm that instead employs a discrete action model on a task defined in MadRTS. As an experimentation platform, we used TIELT (2007), the Testbed for Integrating and Evaluating Learning. TIELT is a free tool that can be used to evaluate the performance of an agent on tasks in an integrated simulation environment. TIELT managed communication between MadRTS and the agents we tested, ran the experiment protocol, and collected results.

We assessed performance in terms of a variant of regret (Kaelbling et al. 1996) that calculates the difference between the performances of two algorithms over time as a percentage of optimal performance. The domain metric measured is the number of steps required to complete the task. As described in Section 2.1, each step corresponds to an order given to a group of units. After 200 steps, a trial is



cut off, so a value of 200 corresponds to failure.

We compared the performance of CASSL versus two baseline algorithms. The first is *random*, which at each time step selects an action randomly from a uniform distribution over the 4-dimensional action space.

The second algorithm is a CMAC controller (Albus 1975), a commonly used algorithm for performing RL tasks in continuous state spaces. It uses a set of overlapping tilings of the state-action space to approximate the RL $Q(s,a)$ function. It executes a query by averaging the value of the tile in each tiling that corresponds to the state-action input. For this experiment, we used five tilings, evenly offset from one another. There are 4 tiles per dimension and 12 dimensions in $S \times A$, which yields a tiling size of 4^{12} and a total of $5 \times 4^{12} = 83.9\text{M}$ tiles. The structure and basic operations of our CMAC are similar to those described in (Santamaria et al., 1998) with $\lambda=0.9$.

For both RL algorithms (CASSL and CMAC), we set

Figure 4: Learning performance

$\alpha=0.2$, $\gamma=1.0$, and $\epsilon=0.5$ (exploration parameter). Both α and ϵ were decreased asymptotically to 0 over time. For CASSL, we also set $\lambda=0$, $k=21$, $\tau_1=0.8$, $\tau_v=0.05$, and $\sigma_1=0.2$. We briefly conducted a manual parameter tuning process to obtain reasonable performances from both algorithms, but did not attempt to optimize their settings.

The MadRTS scenario used for this evaluation has a size of 100 x 100 tiles, each covered with flat terrain. In the starting position, 3 “U.S. Rifleman” (powerful) units controlled by player 1 are clustered around tile $\langle 20, 22 \rangle$, 3 “Insurgent5_AK47” (less powerful) units controlled by player 2 are clustered about $\langle 2, 98 \rangle$, and 1 “Insurgent1_AK47” (powerful) unit controlled by player 2 is at $\langle 98, 2 \rangle$. The victory condition is set to a value of “conquest”, and diplomacy between players 1 and 2 is set to “hostile”. At these settings, the opponent will attempt to hold his ground and destroy all hostile units that enter visual range. All other settings have their default values.

We ran each agent for 10 replications, each on 1000 training trials, and tested on 5 trials after every 25 training trials. We report the average testing results. Although each agent learned on-line within a testing trial, its memory was recorded beforehand and reset after each test. To ensure

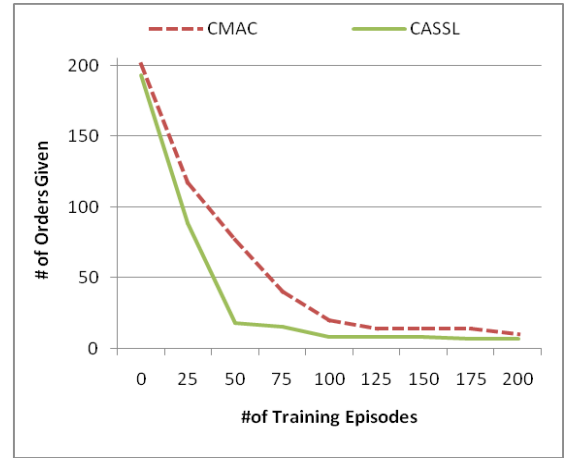


Figure 5: Early learning performance

that trials ended in a reasonable amount of time, we cutoff any that did not complete after 200 time steps; no reward was assigned for the final action of a cutoff trial. A reward of -1 was given at each step unless the agent accomplished its goal (reward=1000) by eradicating the opponent’s units.

Figure 4 displays the results. The curves shown here are monotonically non-increasing because we report the minimum steps taken (per algorithm) on any trial so far in a replication and average over these curves. This measurement is reasonable because prior testing performances can be repeated by restoring the state of the learner; it is more forgiving to algorithms that do not guarantee that learning will never decrease performance.

The regret of CMAC compared to CASSL is 3.53, which is statistically significant ($p=0.001$). Thus, CASSL, using its best learned behavior so far, is 3.53% closer to optimal performance. Comparing CASSL to the random agent, the regret is 38.66, which is again significant ($p < 0.001$).

Figure 5 compares the early learning performance of CMAC and CASSL up to 200 trials. This period is particularly interesting because it shows that CASSL learns to do well earlier than CMAC. The regret during this period (0-200 training trials) is 9.74 with $p=0.017$.

5. Discussion

Our goal was to demonstrate that selecting from among all possible continuous actions rather than a priori reducing their set (e.g., via discretization) can significantly improve performance. However, we assessed this on only a single scenario, and versus only two other algorithms. In future work, we will compare CASSL’s performance, empirically and via a computational complexity analysis, with other algorithms that can process continuous action spaces over a range of learning and performance tasks. This will include variants of CASSL that discretize the action space.

Other models for regression of the local action-value function (e.g., some higher-order polynomial or other function entirely) might outperform the model we used. Also, a model-free variant of CASSL in which the action-value function is represented directly should be studied. The two case bases should scale up to higher dimensions more easi-

ly, but we have not empirically verified this.

We have not optimized CASSL's performance (e.g., employing more selective methods for using neighbors to create action recommendations). This remains future work.

RTS domains often involve a variety of similar tasks with different initial conditions and varied goals. For example, a larger group of units might need to be destroyed at a variety of locations both near and far from the agent's home base. We plan to analyze the capability of CASSL and other RL agents to generalize over different goals and starting conditions in an RTS domain.

6. Conclusions

We introduced a methodology that, unlike our earlier approach (Aha et al. 2005), can learn and reason with continuous action spaces. To do this it integrates case-based reasoning and reinforcement learning methods, and its implementation in CASSL significantly outperformed two baseline approaches on a real-time strategy gaming task.

The primary contribution of this paper was a lazy learning approach for action generation in a continuous space. In our future work, we will compare this approach with variants of CASSL that are eager, that adopt a Q-learning framework, and/or discretize the action space.

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